Image Structure:
Feature Detection and Matching

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Image Intensities

We can represent a monochrome image as a matrix \( I(x, y) \) of intensity values. The size of the matrix is typically 320 × 240 (QVGA), 640 × 480 (VGA), 1280 × 720 (HD) or even as large as 4096 × 2160 (4K) and the intensity values are usually sampled to an accuracy of 8 bits for monochrome images (256 grey levels) or for each the 3 RGB colour channels.

If a point on an object is visible in view, the corresponding pixel intensity, \( I(x, y) \) is a function of many geometric and photometric variables, including:

1. The position and orientation of the camera;
2. The geometry of the scene (3D shapes and layout);
3. The nature and distribution of light sources;
4. The reflectance properties of the surfaces: specular ↔ Lambertian, albedo 0 (black) ↔ 1 (white);
5. The properties of the lens and the CCD.

In practice the point may also only be partially visible or its appearance may be also be affected by occlusion.
**Data reduction**

With current computer technology, it is necessary to discard most of the data coming from the camera before any attempt is made at real-time image interpretation.

\[ \text{images} \rightarrow \text{generic salient features} \]

\[ 10 \text{ MBytes/s} \quad 10 \text{ KBytes/s} \]

(mono CCD)

All subsequent interpretation is performed on the generic representation, not the original image. We aim to:

- Dramatically reduce the amount of data.
- Preserve the useful information in the images (such as the albedo changes and 3D shape of objects in the scene).
- Discard the redundant information in the images (such as the lighting conditions).

We would also like to arrive at a *generic* representation, so the same processing will be useful across a wide range of applications.
Image structure

The answer becomes apparent if we look at the structure of a typical image. In this photo of “Claire”, we’ll examine the pixel data around several patches: a featureless region, an edge and a corner.

0D
The featureless region is characterized by a smooth variation of intensities.
### Edges and corners

#### 1D
The patch containing the edge reveals an intensity discontinuity in one direction.

#### 2D
The patch containing the corner reveals an intensity discontinuity in two directions.

Note that an edge or corner representation imparts a desirable invariance to lighting: the intensity discontinuities are likely to be prominent, whatever the lighting conditions.
1D edge detection

We start with the simple case of edge detection in one dimension. When developing an edge detection algorithm, it is important to bear in mind the invariable presence of image noise. Consider this signal $I(x)$ with an obvious edge.

![Signal](image)

An intuitive approach to edge detection might be to look for maxima and minima in $I'(x)$.

![Differentiated signal](image)

This simple strategy is defeated by noise. For this reason, all edge detectors start by smoothing the signal to suppress noise. The most common approach is to use a Gaussian filter.
1D edge detection

A broad overview of 1D edge detection is:

1. Convolve the signal $I(x)$ with a Gaussian kernel $g_\sigma(x)$. Call the smoothed signal $s(x)$.

$$g_\sigma(x) = \frac{1}{\sigma \sqrt{2\pi}} \exp \left( -\frac{x^2}{2\sigma^2} \right)$$

2. Compute $s'(x)$, the derivative of $s(x)$.

3. Find maxima and minima of $s'(x)$.

4. Use thresholding on the magnitude of the extrema to mark edges.
1D edge detection

The smoothing in step (1) is performed by a 1D convolution:

\[ s(x) = g_\sigma(x) \ast I(x) = \int_{-\infty}^{+\infty} g_\sigma(u)I(x-u) \, du \]

\[ = \int_{-\infty}^{+\infty} g_\sigma(x-u)I(u) \, du \]

The differentiation in step (2) is also performed by a 1D convolution. Thus edge detection would appear to require two computationally expensive convolutions.

However, the derivative theorem of convolution tells us that

\[ s'(x) = \frac{d}{dx} [g_\sigma(x) \ast I(x)] = g'_\sigma(x) \ast I(x) \]

so we can compute \( s'(x) \) by convolving only once — a considerable computational saving.
1D edge detection

Having obtained the convolved signal $s'(x)$, interpolation can be used to locate any maxima or minima to sub-pixel accuracy. Finally, an edge is marked at each maximum or minimum whose magnitude exceeds some threshold.

Looking for maxima and minima of $s'(x)$ is the same as looking for zero-crossings of $s''(x)$. In many implementations of edge detection algorithms, the signal is convolved with the Laplacian of a Gaussian, $g''_\sigma(x)$:

$$s''(x) = g''_\sigma(x) \ast I(x)$$
Zero-crossings

The zero-crossings of $s''(x)$ mark possible edges.

We have not yet addressed the issue of what value of $\sigma$ to use. Consider this signal:

Does the signal have one positive edge or a number of positive and negative edges?
Multi-scale edge detection

Using a small $\sigma$ brings out all the edges.

As $\sigma$ increases, the signal is smoothed more and more, and only the central edge survives.


Multi-scale edge detection

The amount of smoothing controls the **scale** at which we analyse the image. There is no right or wrong size for the Gaussian kernel: it all depends on the scale we're interested in.

Modest smoothing (a Gaussian kernel with small $\sigma$) brings out edges at a fine scale. More smoothing (larger $\sigma$) identifies edges at larger scales, suppressing the finer detail.

This is an image of a dish cloth. After edge detection, we see different features at different scales.

Fine scale edge detection is particularly sensitive to noise. This is less of an issue when analysing images at coarse scales.
2D edge detection

The 1D edge detection scheme can be extended to work in two dimensions. First we smooth the image $I(x, y)$ by convolving with a 2D Gaussian $G_\sigma(x, y)$:

$$G_\sigma(x, y) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$$

$$S(x, y) = G_\sigma(x, y) \ast I(x, y)$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} G_\sigma(u, v) I(x - u, y - v) \, du \, dv$$

The effects of this blurring on a typical image:

Unsmoothed $\sigma = 3$ pixels $\sigma = 4$ pixels
2D edge detection

The next step is to find the gradient of the smoothed image \( S(x, y) \) at every pixel:

\[
\nabla S = \nabla (G_\sigma \ast I)
\]

\[
= \begin{bmatrix}
\frac{\partial (G_\sigma \ast I)}{\partial x} \\
\frac{\partial (G_\sigma \ast I)}{\partial y}
\end{bmatrix}
= \begin{bmatrix}
\frac{\partial G_\sigma}{\partial x} \ast I \\
\frac{\partial G_\sigma}{\partial y} \ast I
\end{bmatrix}
\]

The following example shows \(|\nabla S|\) for a fruity image:

(a) Original image  (b) Edge strength \(|\nabla S|\)
The next stage of the edge detection algorithm is **non-maximal suppression**. Edge elements, or **edgels**, are placed at locations where $|\nabla S|$ is greater than local values of $|\nabla S|$ in the directions $\pm \nabla S$. This aims to ensure that all edgels are located at ridge-points of the surface $|\nabla S|$.

Next, the edgels are **thresholded**, so that only those with $|\nabla S|$ above a certain value are retained.
2D edge detection

The edge detection algorithm we have been describing is due to Canny (1986). The output is a list of edgel positions, each with a strength $|\nabla S|$ and an orientation $\nabla S / |\nabla S|$.

An alternative approach to edge detection was developed by Marr and Hildreth (1980). While the Canny detector is a directional edge finder (both the gradient magnitude and direction are computed), the Marr-Hildreth operator is isotropic. It finds zero-crossings of $\nabla^2 G_\sigma \ast I$, where $\nabla^2 G_\sigma$ is the Laplacian of $G_\sigma$ ($\nabla^2 = \partial^2 / \partial x^2 + \partial^2 / \partial y^2$).
Implementation details

In practice, the image and filter kernels are discrete quantities and the convolutions are performed as truncated summations:

\[
S(x, y) = \sum_{u=-n}^{n} \sum_{v=-n}^{n} G_\sigma(u, v) I(x-u, y-v)
\]

For acceptable accuracy, kernels are generally truncated so that the discarded samples are less than \(1/1000\) of the peak value.

<table>
<thead>
<tr>
<th>(\sigma)</th>
<th>1.0</th>
<th>1.5</th>
<th>3</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>2(n+1)</td>
<td>7</td>
<td>11</td>
<td>23</td>
<td>45</td>
</tr>
</tbody>
</table>

The 2D convolutions would appear to be computationally expensive. However, they can be decomposed into two 1D convolutions:

\[
G_\sigma(x, y) \ast I(x, y) = g_\sigma(x) \ast [g_\sigma(y) \ast I(x, y)]
\]

The computational saving is \((2n+1)^2/2(2n+1)\).
Implementation details

Differentiation of the smoothed image is also implemented with a discrete convolution.

By considering the Taylor-series expansion of $S(x, y)$ it is easy to show that a simple finite-difference approximation to the first-order spatial derivative of $S(x, y)$ is given by:

$$\frac{\partial S}{\partial x} = \frac{S(x+1, y) - S(x-1, y)}{2}$$

This is equivalent to convolving the rows of image samples, $S(x, y)$, with the kernel

$$\begin{bmatrix} 1/2 & 0 & -1/2 \end{bmatrix}$$
Corners

While edges are a powerful intermediate representation, they are sometimes insufficient. This is especially the case when image motion is being analysed. The motion of an edge is rendered ambiguous by the aperture problem: when viewing a moving edge, it is only possible to measure the motion normal to the edge.

To measure image motion completely, we really need to look at corner features. We saw earlier that a corner is characterized by an intensity discontinuity in two directions. This discontinuity can be detected using correlation.
Correlation

The normalized cross-correlation function measures how well an image patch $P(x, y)$ matches other portions of the image, $I(x, y)$, as it is shifted from its original location. It entails sliding the patch over the image, computing the sum of the products of the pixels and normalizing the result:

$$ c(x, y) = \frac{\sum_{u=-n}^{n} \sum_{v=-n}^{n} P(u, v) I(x+u, y+v)}{\sqrt{\sum_{u=-n}^{n} \sum_{v=-n}^{n} P^2(u, v) \sum_{u=-n}^{n} \sum_{v=-n}^{n} I^2(x+u, y+v)}} $$

A patch which has a well-defined peak in its correlation function can be classified as a “corner”.

![Image, I & patch, P](image.png) ![Correlation c(x, y)](correlation.png)
Corner detection

A practical corner detection algorithm needs to do something more efficient than calculate correlation functions for every pixel!

1. Calculate change in intensity in direction \( \mathbf{n} \):

\[
I_n \equiv \nabla I(x, y).\hat{n} \equiv [I_x \ I_y]^T.\hat{n}
\]

\[
I_n^2 = \frac{n^T \nabla I \nabla I^T n}{n^T n}
\]

\[
= \frac{n^T \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} n}{n^T n}
\]

where \( I_x \equiv \partial I/\partial x \) and \( I_y \equiv \partial I/\partial y \).

2. Smooth \( I_n^2 \) by convolution with a Gaussian kernel:

\[
C_n(x, y) = G_\sigma(x, y) * I_n^2
\]

\[
= \frac{n^T \begin{bmatrix} \langle I_x^2 \rangle & \langle I_x I_y \rangle \\ \langle I_x I_y \rangle & \langle I_y^2 \rangle \end{bmatrix} n}{n^T n}
\]

where \( \langle \rangle \) is the smoothed value.
Corner detection

The smoothed change in intensity around \((x,y)\) in direction \(\mathbf{n}\) is therefore given by

\[
C_n(x, y) = \frac{\mathbf{n}^T A \mathbf{n}}{\mathbf{n}^T \mathbf{n}}
\]

where \(A\) is the \(2 \times 2\) matrix

\[
\begin{bmatrix}
\langle I_x^2 \rangle & \langle I_x I_y \rangle \\
\langle I_x I_y \rangle & \langle I_y^2 \rangle
\end{bmatrix}
\]

Elementary eigenvector theory tells us that

\[
\lambda_1 \leq C_n(x, y) \leq \lambda_2
\]

where \(\lambda_1\) and \(\lambda_2\) are the eigenvalues of \(A\). So, if we try every possible orientation \(\mathbf{n}\), the maximum smoothed change in intensity we will find is \(\lambda_2\), and the minimum value is \(\lambda_1\).

We can therefore classify image structure around each pixel by looking at the eigenvalues of \(A\):

**No structure:** (smooth variation) \(\lambda_1 \approx \lambda_2 \approx 0\)

**1D structure:** (edge) \(\lambda_1 \approx 0\) (direction of edge), \(\lambda_2\) large (normal to edge)

**2D structure:** (corner) \(\lambda_1\) and \(\lambda_2\) both large and distinct
Corner detection

The corner detection algorithm we have been describing is due to Harris (1987). It is necessary to calculate $A$ at every pixel and mark corners where the quantity $\lambda_1 \lambda_2 - \kappa (\lambda_1 + \lambda_2)^2$ exceeds some threshold ($\kappa \approx 0.04$ makes the detector a little “edge-phobic”). Note that $\det A = \lambda_1 \lambda_2$ and $\text{trace } A = \lambda_1 + \lambda_2$.

![Low threshold](image1.png) ![High threshold](image2.png)

Corners are most useful for tracking in image sequences or matching in stereo pairs. Unlike edges, the displacement of a corner is not ambiguous. Corner detectors must be judged on their ability to detect the same corners in similar images. Current detectors are not too reliable, and higher-level visual routines must be designed to tolerate a significant number of outliers in the output of the corner detector.
**Blobs**

A *blob* is an area of uniform intensity in the image. Whereas edges and corners are features which are found at discontinuities, blobs are localised in the middle of areas of similar intensity which are surrounded by pixels of a different intensity on their boundaries.

The 1D signal is a scan line running across one of the polka dots above. The result shows how, even though the signal is quite noisy, the minimum of the resulting response from the scale-normalised *Laplacian of the Gaussian* at the correct scale, $\sigma$, localises the centre of the dot perfectly.

$\text{sigma} = 20$
Blobs and Band-pass filtering

The size of the blob detected depends on the sigma of the detector used. As the sigma is increased, larger and larger image features are detected, ranging from small boxes to entire buildings. Each time the blob detector will fire on the center of the blob in question, making it ideal for extracting texture from the inside of an object or for fixing location of an object in the scene.

\[ \sigma = 1 \quad \sigma = 3 \]

\[ \sigma = 7 \quad \sigma = 19 \]
Scale Space

Blobs have a range of scales over which they will be detected. The (scale-normalised) Laplacian of a Gaussian as recorded at a particular location is a smooth function over scale, with definite peaks or troughs. These maxima and minima occur at the centre of blobs. These are considered ideal places to examine the surroundings of the feature point for use in feature description.

\[ \sigma = 5 \]
\[ \sigma = 10 \]
\[ \sigma = 20 \]
\[ \sigma = 40 \]
\[ \sigma = 80 \]
Scale Space, cont.

Different scales are ideal for interest points of different sizes. The ideal scale for a keypoint is the scale corresponding to the maximum of the scale space function at that point. For example, with a blob, we would want to find the maximum of the magnitude of the Laplacian of a Gaussian over scale. The image location of this local max response gives the blob centre position whilst the scale, $\sigma$, defines its size.

To help find the exact point and scale efficiently, a set of discrete scales are sampled (from an Image Pyramid) and the largest value is found by interpolation and then the exact point
We achieve scale independence by looking at the different resolutions (low-pass filtered at different scales) of an image. There are an infinite number of possible resolutions for any image, a three-dimensional function of intensity over location and scale known as the **scale space** of the image, denoted $L(x, y, t)$. This can be calculated by convolving the original image $I(x, y)$ with Gaussians of different scale $t$, thus the scale space function is often written as

\[
L(x, y, t) = G(x, y, t) \ast I(x, y)
\]

\[
G(x, y, t) = \frac{1}{2\pi t} e^{-\left(x^2+y^2\right)/2t}
\]

\[
t = \sigma^2
\]

It is impractical to examine all possible resolutions, and indeed impossible to do so when we are restricted by digital image representation. Thus, we sample the space by choosing particular resolutions to examine.
Scale Space, cont.

We produce a discrete set of low-pass filtered images by smoothing with gaussians with a scale satisfying

\[ \sigma_i = 2^{\frac{i}{s}} \sigma_0 \]

so that it doubles after \( s \) intervals. The \( s \) images in each octave are spaced logarithmically with the scale of neighbouring images satisfying

\[ \sigma_{i+1} = 2^{\frac{1}{s}} \sigma_i \]

Blurring with large scales is avoided in 2 ways: **subsampling** the image after each octave (i.e. scale has doubled) and by using a finite set of **incremental blurs**.

The resulting sampling of spaces is called an **image pyramid**, for which we compute scales ranging from \( \sigma \) to \( 2\sigma \) (an octave), and then subsample the image for the next octave.
Scale Space, cont.

Within each octave, as we convolve images repeatedly with Gaussian filters, the resulting image has a $\sigma$ calculated as

$$G(\sigma_1) * G(\sigma_2) = G\left(\sqrt{\sigma_1^2 + \sigma_2^2}\right)$$

At every interval $i$ of the pyramid, we want $\sigma_i = 2^{i/s}\sigma_0$ (so that it doubles after $s$ intervals). We need to achieve this incrementally, thus

$$G(\sigma_{i+1}) = G(\sigma_i) * G(\sigma_k)$$

So, what is $\sigma_k$?

$$\sigma_k = \sqrt{\sigma_{i+1}^2 - \sigma_i^2}$$

$$\sigma_{i+1} = 2^{i/s}\sigma_i$$

$$\sigma_k = \sqrt{2^{i/s}\sigma_i^2 - \sigma_i^2}$$

$$\sigma_k = \sigma_i\sqrt{2^{2/s} - 1}$$
**Difference of Gaussian**

The **difference of Gaussians** interest point, or DoG as it is often called, is a blob detector. The points are taken from the minima and maxima of the DoG response over an image. It takes its name from the fact that it is calculated as the difference of two Gaussians, which approximates the scale-normalised Laplacian of a Gaussian (see Lowe reference).

\[ G(x, y, k\sigma) - G(x, y, \sigma) \approx (k - 1)\sigma^2\nabla^2 G(x, y, \sigma) \]

In a system which utilizes a scale space pyramid (such as the one we will consider), the DoG point is a useful entity, as a response can be computed simply subtracting one member of a pyramid level from the one directly above it.
Keypoint detection and scale

Keypoint locations (the blob centres) are found by first computing an approximation for the Laplacian of the Gaussian pyramid by using Difference of Gaussians - i.e. subtracting neighbouring images of same dimension in the Image Pyramid. The image location of the local maximum/minimum of the this response (in image position and over scale) gives the feature/keypoint centre and characteristic scale. This will require a local search of 26 neighbour responses to determine if a pixel is a blob-centre and to find the scale.

Figure 1: For each octave of scale space, the initial image is repeatedly convolved with Gaussians to produce the set of scale space images shown on the left. Adjacent Gaussian images are subtracted to produce the difference-of-Gaussian images on the right. After each octave, the Gaussian image is down-sampled by a factor of 2, and the process repeated.
For image matching, blob centres give keypoints which are particularly useful features to concentrate on, as they are usually found inside of objects as opposed to at their edges and thus are less likely to contain part of the background in queries, in addition to other properties such as stability, repeatability, and a definite optimal scale.

The blob centre gives the keypoint image location and the blob scale can be used to normalise for the size/scale of the image feature by sampling the pixels in the neighbourhood of the blob centre at the appropriate image of the Image Pyramid.
To produce a descriptor which is invariant to scale we first normalize for size/scale in the image (by sampling image intensities at the appropriate level of the image pyramid).

We can then normalize for image orientation (by sampling pixels after computing a characteristic reference/dominant orientation for the patch of pixels using a histogram of gradients).

After this geometric size and orientation normalisation we can then compute an appropriate descriptor for each feature by either raw or normalised intensities, edges or the Scale Invariant Feature Transform (SIFT).
Matching intensity patches

The simplest way to describe a patch of an image is just to store the $N$ intensity values, $P[i]$. You can then compare patches directly using cross correlation to find a match.

$$CC(P_1, P_2) = \sum_{i}^{N} P_1[i]P_2[i].$$  \hspace{1cm} (1)

In this raw form the description is not very robust to changes, however.

![Original Patch and Intensity Values](image)

Brightness Decreased, $CC = 0.262720397078039$

Contrast increased, $CC = 0.380413705374859$

Various changes, $CC = 0.297579822063629$
Zero Normalized Patches

Brightness changes are essentially changes in the mean brightness value. While the mean changes, the distribution of the intensity values around the mean stays the same. Thus, by giving the intensity values a zero mean, they become immune to brightness change.

\[ \mu = \frac{1}{N} \sum_{x,y} I(x, y) \]

\[ Z(x, y) = I(x, y) - \mu \]

However, the intensity values are still affected by contrast changes. Contrast is essentially a change in the variance of the distribution of the intensity values around the mean.

Thus, to deal with contrast all that is required is to divide each value by the standard deviation of the intensity value distribution.

\[ \sigma^2 = \frac{1}{N} \sum_{x,y} Z(x, y)^2 \]

\[ ZN(x, y) = \frac{Z(x, y)}{\sigma} \]
Zero Normalized Patches, cont.

The resulting collection of zero-mean, unit variance intensity values is known as a zero-normalized patch, and can be accurately matched using simple cross-correlation. The size of the descriptor grows with the size of the patch, and thus can be quite big. Even so, while not a data reduction, it is a useful way to represent these areas.

![Original Patch and Intensity Values](image)

Brightness Decreased, CC = 0.999988956295594

Contrast increased, CC = 0.969868160814465

Various changes, CC = 0.985010389868036
If you look at the gradient of each pixel in the patch, each will have its own distinct orientation/direction, or way that it is facing, and each will have a size/strength (gradient magnitude).

These can in turn be binned together into an orientation histogram, as shown on the right. Since this histogram is built using gradients/edges, which are robust to contrast and brightness changes and can be detected at different scales, and also incorporates orientation data (thus adding robustness to orientation) this makes them a very strong candidate for a descriptor.
Dominant Orientation

We can find the dominant orientation by looking at the histogram of oriented gradients at the appropriate low-pass filtered image in the Image Pyramid.

We can build a histogram (typically with 36 bins covering 360 degrees) of all of the edge orientations weighted by their gradient magnitudes in the neighbourhood of the keypoint. This needs to be smoothed (low-pass filtered with a 2D gaussian of size $1.5\sigma$ scale for the keypoint).

The highest peak in the histogram will approximate the dominant orientation - a better estimate can be found through interpolation (by fitting a parabola to the values of the bin and its two neighbours). If there is no clear maximum, then the keypoint/interest point is given several dominant orientations (i.e. several copies of the keypoint/interest point with different orientations are used.)

Source Image

Orientation Histogram
The SIFT keypoint descriptor

SIFT stands for Scale-Invariant Feature Transform. It uses a collection of orientation histograms to create a robust and descriptive representation of a patch. This $N \times N$ patch (typically, $N = 16$) is extracted at the scale of the interest point. Thus, while the patch size never changes the area of the actual image it represents changes depending on scale.

The $N \times N$ patch is split into $c$ cells, and within each cell the intensity gradient at every pixel is calculated and the directions binned into a histogram weighted by their magnitude and a Gaussian window with a $\sigma$ of .5 times the scale of the feature centered on the patch. This weights the inner pixels (those closer to the interest point) to avoid possible occlusion problems.
The SIFT keypoint descriptor

If the bins are centered on $d$ directions (typically 8) in each of $c$ cells (typically 16), the resulting descriptor is a $d \times c$ vector (typically 128D).

By dividing the patch into cells, a particular gradient can move around to some degree within the descriptor window and still contribute to the same directional histogram. Once the $d \times c$ vector has been extracted, it is normalized to provide invariance to gradient magnitude change. One final step is performed to help minimize the effects of non-affine lighting changes by thresholding so that all values in the unit vector are less than .2 (to reduce the effect of single elements such as those coming from very strong highlights) and then renormalizing.
Matching features over multiple views

We can use our design of keypoints and their descriptors to build a system to recognize a target object (specified by a reference image) in another viewpoint (query image):

So, one way of solving the correspondence problem is to search through all the feature points (keypoint descriptors) in the database images for the best match of a query feature.

A good match is usually defined as one which is small distance away in feature descriptor space (d=128 for SIFT) as measured by an Euclidean distance metric: following formula

\[ E(\vec{x}, \vec{y}) = \sqrt{\sum_{d} (\vec{x}_d - \vec{y}_d)^2} \]
Finding correspondences - Search

This is called a **linear search**, and is prohibitively expensive to compute. Instead, we must find a way of storing the data to make searching faster.

A data structure organizes data such that it is more efficient to store, access and search. The simplest data structure is a list of items, such as an array of numbers. The most complex are almost impossible to visualize. One solution is to use tree-based data structures such as k-d trees to tackle the problem of nearest neighbour retrieval.
Image Structure: Texture

**Image texture** arises from large numbers of small objects such as grass, brush, pebbles and hair and surfaces with orderly and repetitive patterns such as the spots or stripes on animals, wood and skin. They typically consist of organised patterns of regular sub-elements called *textons*. A natural way to describe texture is to find these textons and describe how they are distributed.

Image textures can be described by their response to a collection of filters to represent the patterns of spots, bars etc.
Characterising Texture

This is an example filter bank. It consists of 8 Laplacian of Gaussian filters and 4 Gaussian filters at different scales to provide non-oriented responses, and 36 oriented filters at 6 different angles, 3 different scales, and 2 different phases. The two phases of oriented filters are first and second derivatives of Gaussians on the minor axis and elongated Gaussians on the major axis, and thus detect edges or bars respectively along their major axes.

The descriptor is simply the concatenated responses of all of the filters in the filter bank at a pixel.
Filter Banks

- Bar
- Brightness
- Bar Filter Response

- Edge
- Blob
- Edge Filter Response
- Blob Filter Response
Filter Banks, cont.

Since filter banks respond to basic image features such as blobs, edges, bars, and average brightness, they are innately immune to most changes in an image.

Original patch

Brightness change

Contrast change

Various changes

Filter Bank Response

No change

Small Change

Medium Change
Learning feature hierarchies

In the previous sections the raw image has been pre-processed through hand-crafted feature extraction (edges, corners, textons). The features were not learned. In many recognition tasks in computer vision we will learn a hierarchy of features just by looking at examples - from low level to mid-level invariant representations to object identities. This is called Deep Learning.
Bibliography

Some of the illustrations in this handout were taken from the following publications, which also make good further reading.

**Edge detection**


**Corner detection**


**Blobs and SIFT descriptor**