Engineering Part IIB: Module 4F11 Speech and Language Processing Lecture 12: Statistical Machine Translation – Alignment Models and Parameter Estimation

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Lent 2014



Cambridge University Engineering Department

Engineering Part IIB: Module 4F11

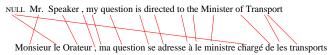
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Word Alignment in Translation

Suppose we have a pair of English and French sentences that are known to be translations. How do the words in one sentence 'generate' the words that make up the other sentence ?

Word Alignments



- A link indicates that the words are translations of each other within these sentences
- Suppose the *i*th English word *e_i* is associated with the *j*th French word *f_j*.
- ► This is indicated by an alignment link (*i*, *j*).
- NULL links : used when simple word-for-word translation is inadequate
- The word alignment of a sentence pair can be specified by an Alignment Link Set.
- Word alignment is also specified by the Alignment Process a_i
- Alignment Links and the Alignment Process are equivalent representations ¹

$$e_i \leftrightarrow f_j \iff b = (i,j) \iff a_j = i \iff e_{a_j} \leftrightarrow f_j$$

Alignment will play a crucial role in defining the Translation Probability.

¹ If each French word is generated by a single English word.



Statistical Models for Word-Level Alignment in Translation Suppose we have an English sentence $E = e_1^t$ and its French translation $F = f_1^t$.

How to define statistical models to assign likelihood to the sentences, i.e. $P(f_1^J | e_1^I)$? Modeling Assumptions:

- Translation has 'direction' : the sentence E = e'_0 generates the sentence F = f'_1
 e₀ is the 'NULL' word
- ► The alignment variable a_1^J indicates the word pairs involved in translation : $e_{a_j} \to f_j$. a_j is an index of the English sentence e_0^J . Therefore a_j takes values in [0, 1, ..., I].
- Introduce the Alignment Process : $P(f_1^J, J|e_0^J) = \sum_{a_1^J} P(f_1^J, J, a_1^J|e_0^J)$
 - note that the French sentence length J is a random variable
- Make simplifying conditional independence assumptions

$$\begin{aligned} P(f_1^J, a_1^J, J | e_0^I) &= P(f_1^J | J, a_1^J, e_0^J) & P(a_1^J | J, e_0^J) & P(J | I) \\ &= \prod_{i=1}^J p_T(f_i | e_{a_i}) & P_A(a_1^J | J, I) & p_L(J | I) \end{aligned}$$

Translation Model Component Distributions

- ► Sentence Length Distribution p_L(J|I)
- Word Translation Distribution $-p_T(f|e)$
- Alignment Distribution $P_A(a_1^J|J, I)$



Sentence Length and Word Translation Distributions

Sentence Length Distribution – $p_L(J|I)$

- Likelihood that an English sentence of *I* words generates *any* Foreign sentence of *J* words
- For specific language pairs, e.g. English→ Chinese, English→French,, relative sentence lengths are fairly predictable. For instance, there tends to be approx. 1.5 Chinese words per English word in translated sentences. Distributions can be tuned to language pairs and translation domains.
- Very simple, but very informative !

Word Translation Distribution $-p_T(f|e)$

- Specifices the likelihood that an English word *e* translates to a foreign word *f*
- Probabilities are maintained in (huge) tables defined for the words in both languages

| English Vocabulary ightarrow

Foreign	$p_T(\text{la} \text{the}) = 0.2$	p_T (maison house) = 0.3	
Vocabulary	$p_T(\text{le} \text{the}) = 0.2$	p_T (bâtiment house) = 0.1	
Ļ	$p_T(\text{les} \text{the}) = 0.25$	p_T (édifice house) = 0.05	
	$p_T(l' the) = 0.25$		
	,		
	•	•	
	•	•	

- Entries are maintained for the likely foreign word translations and a back-off probability is distributed equally over the remaining foreign words
- ► Note that morphological forms are maintained, e.g. Ia, Ie, Ies, I',



Simple Alignment Distributions - IBM Model-1 and Model-2

Alignment Distribution – $P_A(a_1^J|J, I)$

- Assigns probability to the alignment links that describe word alignment
- Specifies the likelihood that any word in the *i*th position in the English sentence is aligned with any word appearing in the *j*th position in the foreign sentence.
- Does not depend on the words in either language (!)

Model-2 makes the following assumption about the alignment process :

$$P_A(a_1^J|J, I) = \prod_{j=1}^J p_{M2}(a_j|j, J, I)$$

- ▶ $p_{M2}(i|j, J, I)$ is stored in tables of dimension $I \times J \times J \times I$ (which can be simplified)
- alignment links are independent of each other
- the link distribution depends on the foreign word location j

<u>Model-1</u> assumes that the component distribution is entirely flat : $p_{M2}(a_j|j, J, I) = \frac{1}{I}$

$$P_A(a_1^J|J,I)=\frac{1}{I^J}$$

- Special case of Model-2
- Likelihood of a collection of links a_1^J depends only on the number of links J



Incorporating Hidden Markov Models Into Word Alignment

One of the weaknesses of the Model-1 and Model-2 alignment process is due to the harsh conditional independence assumptions made within the alignment component :

$$P(a_1^J|J, I, e_0^J) \approx \prod_{j=1}^J P_A(a_j|j, J, I)$$

A consequence of this assumption is that the alignment of individual foreign words is determined independently of the alignment of their neighbors, e.g. alignment of any Foreign word f_j is independent of the alignment of either f_{j-1} or f_{j+1} .

The HMM Word Alignment Model strengthens the overall alignment model by introducing a first-order Markov process into the Alignment Distribution :

$$P_A(a_1^J|J, I) = \prod_{j=1}^J P(a_j|a_1^{j-1}, J, I) \approx \prod_{j=1}^J p_{HMM}(a_j|a_{j-1}, I)$$

- Markov Position Alignment Distribution : $p_{HMM}(a_j|a_{j-1}, I)$
- Each link in the alignment sequence depends on the previous link.
- The overall process is an HMM
- ► Note that Model-1 and Model-2 are (almost) special cases of HMM Alignment



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Example – Generation of HMM Word Alignments

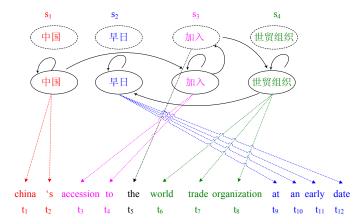


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t_1	t_2	t ₃	t4	t5	t ₆	t7	t ₈	t9	t_{10}	t_{11}	t ₁₂

States are associated with the words on the 'generating' side



Example – Generation of HMM Word Alignments



States are associated with the words on the 'generating' side State sequences are generated and determine the word-to-word alignments Words are generated one by one, one word with each state transition States can occur multiple times in an alignment sequence



Summary of IBM Model-1, Model-2, and HMM Word Alignment

Step 1. Specify the foreign sentence length J under $P_L(J|I)$

Step 2. Generate a word alignment sequence of length J

$$\underline{\text{Model 1}}: P_A(a_1^J \mid e_0^I, J) = \frac{1}{(I+1)^J}$$

Model 2:
$$P_A(a_1^J | e_0^I, J) = \prod_{j=1}^J p_{M2}(a_j | j, J, I)$$

HMM:
$$P_A(a_1^J | e_0^I, J) = \prod_{j=1}^J p_{HMM}(a_j | a_{j-1}, I)$$

Step 3. Generate the foreign sentence from the aligned English words:

$$P(f_1^J \mid a_1^J, e_0^I) = \prod_{j=1}^J p_T(f_j \mid e_{a_j})$$

Overall Translation Probability Under Each Model:

$$P(t_1^J, a_1^J, J|e_0^J) = \frac{1}{(I+1)^J} p_L(J|I) \prod_{j=1}^J p_T(f_j|e_{a_j}) - \text{Model-1}$$

$$P(t_1^J, a_1^J, J|e_0^J) = p_L(J|I) \prod_{j=1}^J p_T(f_j|e_{a_j}) p_{M2}(a_j|j, J, I) - \text{Model-2}$$

$$P(t_1^J, a_1^J, J|e_0^J) = p_L(J|I) \prod_{j=1}^J p_T(f_j|e_{a_j}) p_{HMM}(a_j|a_{j-1}, I) - \text{HMM}$$



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Automatic Alignments and Translation Probability

Suppose we have an alignment model - either Model-1, Model-2, or an HMM Suppose we also have a pair of sentences (e_1^ℓ, f_1^J) which we know are translations. We can use these models to find Automatic Alignments of the known translations.

$$\widehat{a}_1^J = \operatorname*{argmax}_{a_1^J} P(f_1^J, a_1^J, J, |e_1^I)$$

We can also carry out efficient marginalization over all alignments to find the translation probability

$$P(f_1^J|e_1^I) = \sum_{a_1^J} P(f_1^J, a_1^J, J, |e_1^I)$$

► With Model-1, Model-2, and the HMM, these operations can be carried out either by the Viterbi procedure or the Forward-Backward Algorithm, respectively.



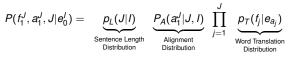
Parameter Estimation in Word Alignment Models

The basic models used in word alignment were defined in the previous lecture

IBM Model-1, IBM Model-2, Alignment HMM

The general forms of the alignment models are specified by their component distributions

• Probability that a foreign sentence $F = f_1^J$ is a translation of an English sentence $E = e_0^J$:



We have a collection of training sentences: $\{F^{(r)}, E^{(r)}\}_{r=1}^{R} \leftarrow Sentence Aligned Parallel Text$

How can the component models be estimated from the example translations ?

Sentence Length Distribution :

Easy to estimate from sentence-level statistics:

$$P_L(J|I) = \frac{\sum_{r=1}^R 1(J = J^{(r)}, I = I^{(r)})}{\sum_{r=1}^R 1(I = I^{(r)})}$$

 \rightarrow a distribution based on a simple sentence length ratio also works well



Word Translation Distributions from Word Alignments

Recall that word aligned sentences can be represented by a set of Word Alignment Links

$$e_i \leftrightarrow f_j \iff a_j = i \iff e_{a_j} \leftrightarrow f_j$$

NULL Mr. Speaker, my question is directed to the Minister of Transport

Monsieur le Orateur , ma question se adresse à le ministre chargé de les transports

Word Translation Distribution :

How do we estimate $P_T(f | e)$ from word-aligned sentences $\{F^{(r)}, E^{(r)}, a^{(r)}\}_{r=1}^R$? $a^{(r)} = [a_1^{(r)}, \dots, a_{j(r)}^{(r)}] \leftarrow \text{word alignments for } F^{(r)}, E^{(r)}$

Step 1 : Count the number of times a foreign word f is aligned to an English word e

$$\#_{T}(f \leftrightarrow e) = \sum_{r=1}^{R} \sum_{j=1}^{J^{(r)}} \sum_{i=1}^{I^{(r)}} \underbrace{1(e = e_{i}^{(r)})}_{e \text{ is the } i^{th}} \underbrace{1(f = f_{j}^{(r)})}_{f \text{ is the } j^{th}} \underbrace{1(a_{j}^{(r)} = i)}_{e_{j}^{(r)} \leftrightarrow f_{j}^{(r)}}$$

Step 2 : Compute the Word Translation Distribution:

$$P_{T}(f|e) = \frac{\#_{T}(f\leftrightarrow e)}{\sum_{f'} \#_{T}(f'\leftrightarrow e)}$$



Word Translation Distributions from Word Alignments - An Example Two aligned sentence pairs : R = 2, $I^{(1)} = I^{(2)} = 5$, $J^{(1)} = J^{(2)} = 4$



Estimation of Model-2 Alignment Distribution

Model-2 Position Alignment Distribution : $P_A(a_1^J|J, I) = \prod_{j=1}^J p_{M2}(a_j|j, J, I)$

How do we estimate $p_{M2}(i | j, J, I)$ from word-aligned sentences ?

Step 1 : Accumulate position alignment statistics over the word-aligned sentences

$$\#_{M2}(i, j, J, I) = \sum_{r=1}^{R} 1(J = J^{(r)}, I = I^{(r)}) \sum_{j=1}^{J} \underbrace{1(i = a_{j}^{(r)})}_{a_{i}^{(r)} \leftrightarrow f_{j}^{(r)}}$$

 \rightarrow How often is position i linked with position j in sentences of length J and I.

Step 2 : Compute the Position Alignment Distribution

$$p_{M2}(i|j,J,l) = \frac{\#_{M2}(i,j,J,l)}{\sum_{i''=1}^{l} \#_{M2}(i'',j,J,l)}$$

 \rightarrow Probability of linking position j to position i in sentences of length J and I.



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Estimation of Model-2 Alignment Distribution - An Example Two aligned sentence pairs : R = 2, $I^{(1)} = I^{(2)} = 5$, $J^{(1)} = J^{(2)} = 4$

Note that the alignment probabilities depend only on the word alignment information. The identity of the words in each position in the sentence does not play a role once the alignments are generated.



Estimation of HMM Alignment Distribution

Markov Position Alignment Distribution : $P_A(a_1^J|J, I) = \prod_{j=1}^J p_{HMM}(a_j|a_{j-1}, I)$

Step 1 : Accumulate position-to-position occurrence statistics over the alignments

$$\#_{HMM}(i, i', l) = \sum_{r=1}^{R} 1(l = l^{(r)}) \sum_{j=1}^{J^{(r)}} \underbrace{1(i' = a_{j-1}^{(r)}, i = a_{j}^{(r)})}_{e_{i'}^{(r)} \leftrightarrow f_{j-1}^{(r)} \text{ and } e_{i}^{(r)} \leftrightarrow f_{j}^{(r)}}$$

ightarrow Number of links to position i' followed by links to i in English sentences of length I .

Step 2 : Compute the Markov Position Alignment Distribution from these occurrence statistics

$$p_{HMM}(i | i', l) = \frac{\#_{HMM}(i, i', l)}{\sum_{i''=1}^{l} \#_{HMM}(i'', i', l)}$$

ightarrow Probability of linking to position i after a link to i' in an English sentence of length I .



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Estimation HMM Alignment Distribution - An Example Two aligned sentence pairs : R = 2, $I^{(1)} = I^{(2)} = 5$, $J^{(1)} = J^{(2)} = 4$

 $#_{HMM}(i, i', I)$: number of times *i* follows *i'* in the word alignments

- easily computed from the reordered English word index sequences 2, 1, 3, 5 and 3, 0, 2, 4

 $\begin{array}{l} \#_{HMM}(i=1,i'=2,l=5)=1 \\ \#_{HMM}(i=4,i'=2,l=5)=1 \\ \#_{HMM}(i=5,i'=3,l=5)=1 \\ \#_{HMM}(i=0,i'=3,l=5)=1 \\ & p_{HMM}(a_{j}=5|a_{j-1}=3,l=5)=\frac{1}{2} \\ \#_{HMM}(i=0,i'=3,l=5)=1 \\ & p_{HMM}(a_{j}=0|a_{j-1}=3,l=5)=\frac{1}{2} \\ & \sum_{i''=1}^{l=5} \#_{HMM}(i'',i'=3,l=5)=2 \\ & \sum_{i''=1}^{l=5} \#_{HMM}(i'',i'=3,l=5)=2 \\ \end{array}$



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Automatic Word Alignments and Iterative Parameter Estimation Viterbi Alignment can be performed for : IBM Model-1 , IBM Model-2 , and the HMM

$$\widehat{a}_1^J = \operatorname*{argmax}_{a_1^J} P(f_1^J, a_1^J \mid e_0^J)$$

Flat Start Training Procedure: Gradually increase the complexity of the alignment distribution

- 1. Model-1
 - 1.1 Model-1 Initialization set $p_T(f|e)$ to be uniform
 - 1.2 Perform initial Model-1 Viterbi alignment to generate word aligned parallel text
 - 1.3 Update $p_T(f|e)$ from the word-aligned parallel text
 - 1.4 Perform Model-1 Viterbi alignment to generate word aligned parallel text
 - 1.5 Return to Step 1.3 until some stopping criteria is met
 - 1.6 Output: Model-1 word-aligned parallel text
- 2. Model-2
 - 2.1 Model-2 Initialization find $p_{M2}(i|j, J, I)$ and $p_T(f|e)$ using the word-alignments from Step 1.6
 - 2.2 Perform Model-2 Viterbi alignment to generate word aligned parallel text
 - 2.3 Update $p_{M2}(i|j, J, I)$ and $p_T(f|e)$ from the word-aligned parallel text
 - 2.4 Return to Step 2.2 until some stopping criteria is met
 - 2.5 Output: Model-2 word-aligned parallel text
- 3. HMM
 - 3.1 HMM Initialization find $p_{HMM}(i|i', I, J)$ and $p_T(f|e)$ using the word-alignments from Step 2.5
 - 3.2 Perform HMM Viterbi alignment to generate word aligned parallel text
 - 3.3 Update $p_{HMM}(i|i', I, J)$ and $p_T(f|e)$ from the word-aligned parallel text
 - 3.4 Return to Step 3.2 until some criteria is met
 - 3.5 Perform a final HMM Viterbi alignment to generate word aligned parallel text
 - 3.6 Output: HMM parameters and word-aligned parallel text



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Iterative Alignment Model Parameter Estimation by EM This estimation procedure uses 'hard counts' extracted from word alignments.

For example, the Word Translation Distribution relies on the function $1(a_j^{(r)} = i)$ which specifies that $f_j^{(r)} \leftrightarrow e_i^{(r)}$.

$$\#(f \leftrightarrow e) = \sum_{r=1}^{R} \sum_{j=1}^{J^{(r)}} \sum_{i=1}^{I^{(r)}} 1(e = e_i^{(r)}) 1(f = f_j^{(r)}) \underbrace{1(a_j^{(r)} = i)}_{e_i^{(r)} \leftrightarrow f_j^{(r)}}$$

EM replaces 'hard counts' by posterior probabilities

$$\#(f \leftrightarrow e) = \sum_{r=1}^{R} \sum_{j=1}^{J^{(r)}} \sum_{i=1}^{I^{(r)}} 1(e = e_i^{(r)}) 1(f = f_j^{(r)}) \underbrace{P(a_j^{(r)} = i \mid E^{(r)}, F^{(r)})}_{P(e_i^{(r)} \leftrightarrow f_j^{(r)} \mid E^{(r)}, F^{(r)})}$$

The Word Translation distribution is found as before, but with the posterior probabilities

$$P_T(f|e) = \frac{\#(f \leftrightarrow e)}{\sum_{f'} \#(f' \leftrightarrow e)}$$

and estimation formulae for the Model-2 and HMM alignment distributions are similar.

Posterior probabilities are easy to compute under the HMM - very similar to ASR



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IBM Model-4 for Word Alignment

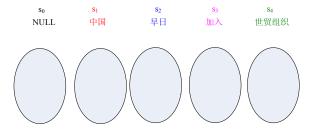
Model 4 is a powerful model of word alignment within sentence pairs Features:

- Lexical translation model: as in Model 1 and HMM alignment model
- Fertility: probability distribution over the number of French words each English word can generate
 - an approximation to phrase modeling
- NULL Translation Model: allows French words to be generated without a corresponding source on the English side
- Distortion Model: describes how French words are distributed throughout the French sentence when generated from a single English word



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Model-4 Generation: Step 1 – Tablets



Create a tablet for each source word



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Model-4 Generation: Step 2 – Fertility

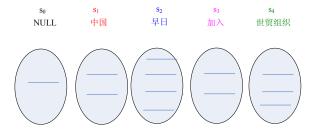
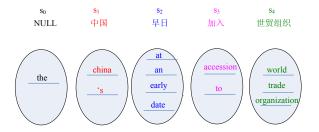


Table lookup to decide fertility: # of target words connected



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Model-4 Generation: Step 3 – Fill in Tablet Positions

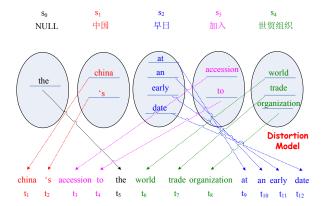


Sample target words from translation table i.i.d.



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Model-4 Generation: Step 4 - Fill in the English Sentence





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IBM Model-4 Summary

Very powerful model of word alignment in translated sentences

Fertility and Distortion begin to capture generation of phrases in translation.

Model-4 has several shortcomings

- Deficiency The Distortion Model used to move words from the tables into position in the sentence may place two words in one sentence position. This is a drawback - some probability mass under the model is assigned to what are effectively non-sentences. The probabilities over alignments and generated sentences do not sum to 1.0. The models are therefore called deficient.
- Parameter estimation and word alignment is difficult to implement
 - Unlike Model-1, Model-2, and HMM Alignment, dynamic programming based algorithms are not available for Model-4

It is difficult to balance modeling power against computational efficiency in alignment.

Despite these difficulties, IBM Model-4 can be used to generate high-quality word alignments over parallel text, especially as implemented under the GIZA++ toolkit². However, it doesn't parallelize as easily other models.



²http://www.fjoch.com/GIZA++.html Engineering Department

Cambridge University

Document Level Alignment

The definition of a document varies. Depending on the domain, a document could be a book, a news story, a numbered chapter, paragraph, or verse, ...

Parallel Documents are created purposefully by human translators, for example in creating a foreign language edition of a newspaper.

- correspondence between the translations and the original source language documents is maintained
- these are the most valuable, but are expensive to create and to obtain
- large collections of parallel documents are available from LDC

Some interest in searching for Parallel Documents 'in the wild' by crawling the web and looking for hints that documents encountered might be translations of each other.

... assume we have parallel documents

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Document and Sentence Aligned Parallel Text

Parameter estimation procedures discussed so far require sentence-level translations for use as a training set. However, most parallel texts are available as documents.

The definition of a document varies. Depending on the domain, a document could be a book, a news story, a numbered chapter, paragraph, or verse, ...

English Document

[1] Perhaps the Commission or you could clarify a point for me. [2] It would appear that a speech made at the weekend by Mr Fischler indicates a change of his position. [3] I welcome this change because he has said that he will eat British beef [4] and that the ban was imposed specifically for economic and political reasons. [5]

French Document

 La Commission ou vous-même pourriez peutêtre m'expliquer un point.
 Il semblerait en effet que M. Fischler ait changé de position dans un discours prononcé au cours de ce week-end.
 Je me félicite de ce changement, car il a dit qu'il mangerait du boeuf britannique [4] et que l'interdiction avait été décrétée spécifiquement pour des raisons économiques et politiques.

Automatic Sentence Alignment:

Given a pair of documents, the goal of Sentence Alignment is to extract subsequences of text that are mutual translations. These may be sentences, sub-sentences, or multiple sentences.

- 'Markers' are inserted into the text to indicate possible translation boundaries
- Translation segments can be sub-sentence units, e.g. at [4]. As a result some aligned 'sentences' might be sub-sentence fragments.
- Segments can be discarded as spurious text without a corresponding translation

Aligned segments can be extracted and used for estimation of word alignment models.



Automatic Sentence Alignment Procedures

An Alignment Grid defines the possible segment alignments between two documents

A path defines both segmentation and alignment

Segment Alignment Specified by Path (a)

- $E^{(1)}E^{(2)}$ are merged and aligned with $F^{(1)}$
- $E^{(3)}$ is deleted
- $E^{(4)}$ is aligned to $F^{(2)}$
- $F^{(3)}F^{(4)}$ are merged and aligned with $E^{(5)}$

Alignment is based on two underlying processes :

- (1) A probability distribution defined over alignment paths. Paths near the diagonal with shorter segments are preferred
- (2) A translation probability defined over aligned segment pairs 4 Sentences
 - Employs a simple model such as IBM Model-1 with a sentence length component

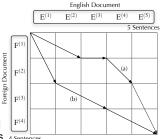
The two scores are combined to assign a probability to a particular segmentation and alignment of the document pairs.

Monotone Segment Alignment

Dynamic programming search finds the most likely alignment of translation segments.

- Simple translation models (e.g. Model-1) are used so that large amounts of parallel documents can be sentence-aligned efficiently
- The alignment is monotone: segments may be deleted but not reordered. This prevents the search space from growing too large.





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Sentence Alignment Goal: Better Word Translation Models

Benefits of good sentence alignment

- better training set alignment improves translation performance
- shorter aligned segments leads to faster translation model training
- A good alignment algorithm should be ...
 - fast , so multiple iterations are possible
 - efficient: as little bitext should be discarded as possible
 - initialized from a flat-start
 - language independent
 - require minimal linguistic knowledge
 - able to work at the subsentence level
 - coarse monotonic alignment followed by fine divisive clustering works well
 - splitting points can depend on the language pairs

